

Examination 1
September 19, 2008

1. (50 points) Define and/or characterize

- a. photon

a particle of light (or electromagnetic radiation) characterized by a frequency ν , wavelength λ & energy $E = h\nu = \frac{hc}{\lambda}$

- b. line spectrum

when a atom falls from a higher energy level to a lower one it will emit radiation characteristic of the discrete energy difference between the atoms energy levels. the collection of these frequencies is a line spectrum

- c. node

a point where a function is zero.

- d. Bohr orbit

In the Bohr theory of the H atom the electron moves in a circular orbit of radius $a_0 = 0.5291772 \text{ \AA}$. This is called the Bohr orbit.

- e. Kronecker delta

A symbol δ_{ij} defined so that

$$\delta_{ij} = \begin{cases} 0 & \text{if } i \neq j \\ 1 & \text{if } i = j \end{cases}$$

useful in designating orthogonal functions that are also normalized

- f. correspondence principle

when the quantum numbers associated with a system become very large the system begins to behave as it would classically.

- g. Hamiltonian for a particle confined to a cube

$$\hat{H} = -\frac{\hbar^2}{2m} \nabla^2 = -\frac{\hbar^2}{2m} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right)$$

- h. Harmonic oscillator

A system in which a particle is attracted to the origin with a force that depends linearly on the displacement from the origin. $F = -kx$.

Results in a potential energy $V = \frac{1}{2} kx^2$.

- i. stationary state

If the solution to the time dependent wave Hamiltonian is $\psi = \psi_n(x) e^{-iE_n t/\hbar}$ where

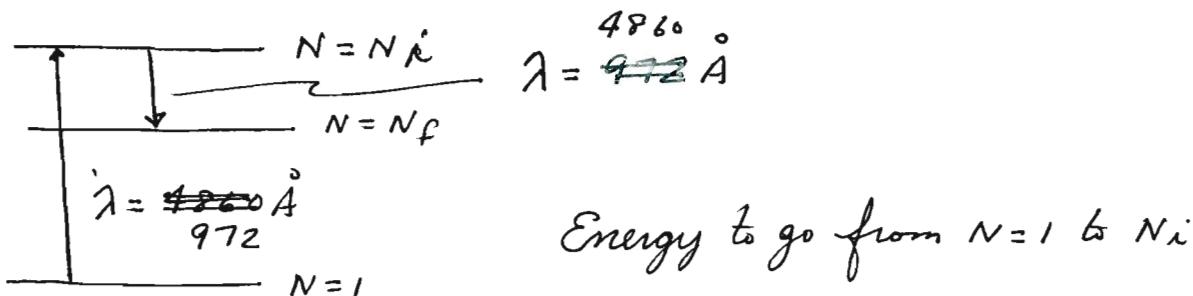
$$\hat{H} \psi_n = E_n \psi_n \text{ thus } \psi^* \psi = \psi_n^* (x) \psi_n(x)$$

& ψ is a stationary state.

- j. eigenfunction

given an operator \hat{A} & a function f
 if $\hat{A}f = \lambda f$ where λ is a constant
 then f is an eigenfunction of \hat{A} .

2. (15 points) A ground-state hydrogen atom absorbs a photon of light that has a wavelength of 97.2 nm. It then gives off a photon that has a wavelength of 486 nm. What is the final state of the hydrogen atom?



Energy to go from $N=1$ to N_i

$$\frac{12399}{972} = 12.75 \text{ eV}$$

$$\therefore \Delta E = -13.6057 \left(\frac{1}{N_\lambda^2} + \frac{1}{1} \right) = -12.75$$

$$\frac{1}{N_\lambda^2} = 1 - 0.9371 = 0.0629$$

$$N_\lambda \approx 4$$

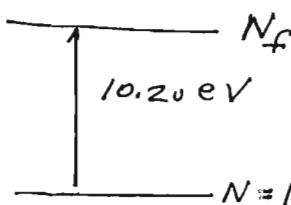
emission $\Delta E = -13.6057 \left(\frac{1}{N_f^2} - \frac{1}{16} \right) = -2.55$

$$\frac{12399}{4860} = 2.55 \text{ eV}$$

$$\frac{1}{N_f^2} = 0.1875 + \frac{1}{16} = 0.25$$

$$N_f = 2.0$$

or the atom winds up in the state which is 10.20 eV above ground state



$$\Delta E = -13.6057 \left(\frac{1}{N_f^2} - 1 \right) = 10.20$$

$$\frac{1}{N_f^2} = 0.25$$

$$N_f = 2$$

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3. (10 points) Given that the work function of Chromium is 4.40 eV, calculate the kinetic energy (in eV) of the electrons emitted from a Chromium surface that is irradiated with ultraviolet radiation of wavelength 200 nm.

$$E = KE + W$$

$$W = 4.40 \text{ eV}$$

$$E = \frac{12399}{2000} = 6.2 \text{ eV}$$

$$W = 6.2 - 4.4 = 1.8 \text{ eV}$$

4. (10 points) In each case, show that $f(x)$ is an eigenfunction of the operator given. Find the eigenvalue.

	Operator	$f(x)$	<i>eigenvalue</i>
(a)	$\frac{d^2}{dx^2}$	$\cos \omega x$	$-\omega^2$
(b)	$\frac{d}{dt}$	$e^{i\omega t}$	$i\omega$
(c)	$\frac{d^2}{dx^2} + 2\frac{d}{dx} + 3$	e^{ax}	$a^2 + 2a + 3$
(d)	$\frac{\partial}{\partial y}$	$x^2 e^{6y}$	6

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5.(15 points) The force constant of $^{79}Br^{79}Br$ is 240 Nm^{-1} . Calculate the fundamental vibrational frequency and the zero-point energy of $^{79}Br^{79}Br$.

$$\nu = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} \quad \mu = \frac{M}{2} = \frac{79}{2} (1.661 \times 10^{-27}) \text{ kg}$$

$$\nu = \frac{1}{2\pi} \sqrt{\frac{(240)(2)}{(79)(1.661)} \times 10^{-27}} = \frac{1}{2\pi} \sqrt{36.58 \times 10^{-26}}$$

$$\nu = \frac{6.048}{2\pi} \times 10^{13} \text{ Hz} = 0.963 \times 10^{13} \text{ Hz}$$

$$E = \frac{h\nu}{2} = \frac{(6.626)(0.963) \times 10^{-34+13}}{2} \text{ J} = 3.19 \times 10^{-21} \text{ J}$$

$$\Delta E \text{ ev} \quad \frac{3.19 \times 10^{-21} \text{ J}}{1.602 \times 10^{-19} \text{ J/eV}} = 1.99 \times 10^{-2} \text{ eV} \approx .02 \text{ eV}$$