

# Binary phase shaping for selective single-beam CARS spectroscopy and imaging of gas-phase molecules

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**We report on mode-selective single-beam coherent anti-Stokes Raman scattering spectroscopy of gas-phase molecules. Binary phase shaping (BPS) is used to produce single-mode excitation of O<sub>2</sub>, N<sub>2</sub>, and CO<sub>2</sub> vibrational modes in ambient air and gas-phase mixtures, with high-contrast rejection of off-resonant Raman modes and efficient nonresonant-background suppression. In particular, we demonstrate independent excitation of CO<sub>2</sub> Fermi dyads at ~1280 and ~1380 cm<sup>-1</sup> and apply BPS for high-contrast imaging of CO<sub>2</sub> jet in ambient air. Copyright © 2010 John Wiley & Sons, Ltd.**

**Keywords:** pulse shaping; selective excitation; pseudorandom binary phase; standoff detection; spectroscopy

## Introduction

Recent advances in pulse shaping and ultrafast laser technologies have brought coherent nonlinear optical techniques toward an outstanding level of laser-field control and functionality. Starting with the early work by Nelson and Weiner on pulse-sequence generation for enhanced impulsive stimulated Raman scattering in solids,<sup>[1,2]</sup> the use of pulse shapers has led to a variety of novel nonlinear optical techniques. Single-beam (single-pulse) coherent anti-Stokes Raman scattering (CARS) spectroscopy, first demonstrated for microscopy,<sup>[3]</sup> is one prominent example.

CARS is a third-order process that relies on coherent excitation of Raman active molecular vibrations.<sup>[4]</sup> The molecules are excited via pump and Stokes fields. The induced oscillations are then probed by a third laser pulse. The traditional implementation involves three laser beams of at least two different wavelengths that are overlapped in a phase-matched BOXCAR geometry and properly timed. In single-beam CARS, the pump, Stokes, and probe components are encompassed within a single broadband laser spectrum. Pulse shaping is then utilized to implement various strategies for background suppression, signal enhancement, and excitation selectivity if needed.

In their original work on single-beam CARS, Dudovich *et al.*<sup>[3]</sup> used a sinusoidal phase modulation both to gain selectivity and to suppress the nonresonant contribution. Silberberg's group also showed that a simple  $\pi$ -phase gate can give a certain degree of discrimination between the resonant and nonresonant contributions to the CARS spectra.<sup>[5]</sup> They soon followed with a demonstration of a phase-and-polarization shaping technique, which offered superior nonresonant-background suppression while preserving the multimode character of impulsive Raman excitation.<sup>[6]</sup> Another way of using both phase and polarization control was devised by Leone's group,<sup>[7]</sup> who employed the homodyne mixing of the resonant signal with the nonresonant background to improve the detection limit. This was followed with a heterodyne detection scheme for single-beam CARS by von Vacano *et al.*<sup>[8]</sup> Note that, due to both phase-matching

considerations (relaxed phase-matching constrains under high-NA focusing) and the lack of high-power sub-10-fs laser sources, the original focus of single-beam CARS techniques was microscopy. Dantus's group was the first to transfer this technology for standoff detection of vapors, liquids, and powdered samples.<sup>[9,10]</sup> It was also found valuable for CARS spectroscopy of combustion-related gases.<sup>[11]</sup>

As pointed out above, selective excitation of Raman modes facilitates nonresonant-background suppression in the single-beam CARS scheme. Importantly, it also allows elimination of multi-channel acquisition of CARS spectra, which is difficult to integrate with high-speed laser beam scanning for imaging applications. The aforementioned sinusoidal phase modulation, though conceptually simple, provides a fairly low degree of signal rejection at off-resonant Raman frequencies. Better contrast is expected for linearly chirped pulses that have been utilized extensively in multi-beam CARS setups.<sup>[12–14]</sup> Another attractive alternative, discussed in this work, is pseudorandom binary sequences. Using pseudorandom binary phase shaping (BPS), we have demonstrated previously high-contrast excitation selectivity for second-harmonic generation, two-photon excited fluorescence, and stimulated Raman scattering.<sup>[15]</sup> We have also applied BPS for mode-selective CARS in liquid samples.<sup>[9]</sup> Here we extend it to selective excitation of gas-phase molecules. In particular, we use pseudorandom BPS

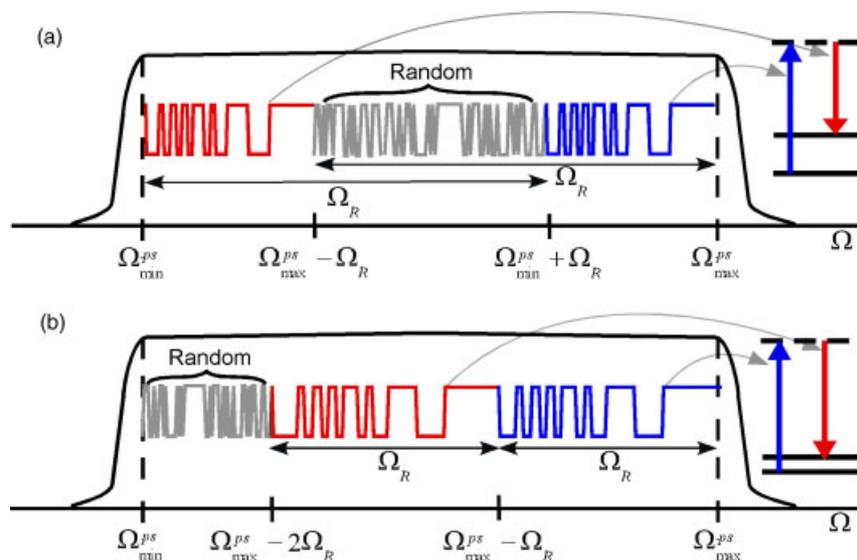
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**Figure 1.** Selective excitation of Raman active vibrational modes via BPS: (a) binary phase mask design for  $\Delta\Omega^{\text{PS}} < 2\Omega_R$ ; (b) binary phase mask design for  $\Delta\Omega^{\text{PS}} \geq 2\Omega_R$ . Here  $\Delta\Omega^{\text{PS}}$  is the bandwidth of the pump Stokes part of the laser spectrum;  $\Omega_R$  is the transition Raman shift.

for selective excitation of  $\text{O}_2$  ( $\sim 1550 \text{ cm}^{-1}$ ) and  $\text{N}_2$  ( $\sim 2330 \text{ cm}^{-1}$ ) vibrations in ambient air. We also show independent excitation of  $\text{CO}_2$  Fermi dyads at  $\sim 1280$  and  $\sim 1380 \text{ cm}^{-1}$  in gas-phase  $\text{CO}_2$  and  $\text{CO}_2/\text{N}_2$  mixtures. Finally, we demonstrate selective single-beam CARS imaging of  $\text{CO}_2$  gas jet.

## BPS for Selective Single-Beam CARS

Coherent vibrations of a molecular ensemble in CARS are established through the nonlinear interaction with the optical field. The excitation efficiency is, therefore, dependent on both the amplitude and the relative phase of contributing spectral components, or rather on multiphoton intrapulse interference since the excitation is impulsive.<sup>[16,17]</sup> The coherence amplitude at some wavenumber  $\Omega_R$  is proportional to

$$E^{(0)}(\Omega_R) \equiv \int_0^{+\infty} E(\Omega + \Omega_R)E^*(\Omega)d\Omega \quad (1)$$

where  $E(\Omega) \equiv |E(\Omega)| \exp[i\varphi(\Omega)] \propto \sqrt{S(\Omega)} \exp[i\varphi(\Omega)]$  is a complex spectral amplitude of the field at wavenumber  $\Omega$ , determined by the spectral field intensity  $S(\Omega)$  and phase  $\varphi(\Omega)$ . Since the pulse shaper operates with a finite number of independent channels, it is insightful to rewrite Eqn (1) for a mesh of  $N$  equidistantly spaced points between  $\Omega_{\text{min}}^{\text{PS}}$  and  $\Omega_{\text{max}}^{\text{PS}}$ :

$$E_n^{(0)} \equiv \sum_{m=0}^{N-n-1} E_{m+n} E_m^* \propto \sum_{m=0}^{N-n-1} \sqrt{S_{m+n} S_m} \exp[i(\varphi_{m+n} - \varphi_m)], \quad n = 0, \dots, N-1 \quad (2)$$

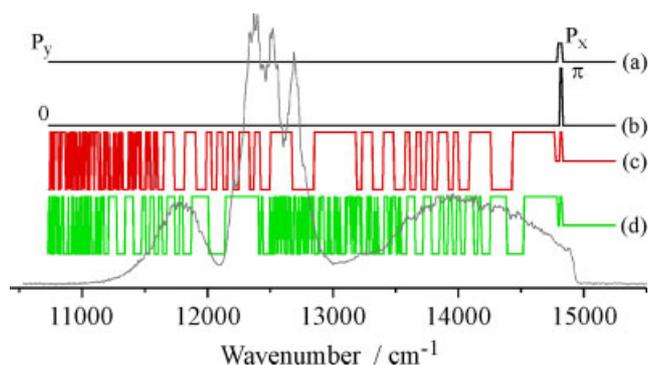
The notations used are:

$$\begin{aligned} E_j^{(0)} &= E^{(0)}(j\Delta\Omega_N), E_j \equiv E(\Omega_j), S_j \equiv S(\Omega_j), \varphi_j \equiv \varphi(\Omega_j), \\ \Omega_j &= \Omega_{\text{min}}^{\text{PS}} + j\Delta\Omega_N, \Delta\Omega_N = (\Omega_{\text{max}}^{\text{PS}} - \Omega_{\text{min}}^{\text{PS}})/(N-1), \\ j &= 0, \dots, N-1 \end{aligned} \quad (3)$$

If we now limit the phase values to 0 or  $\pi$  (more generally, to two values offset by  $\pi$ ) and assume that the spectral intensity

within the  $[\Omega_{\text{min}}^{\text{PS}}, \Omega_{\text{max}}^{\text{PS}}]$  interval remains constant, we find that the electric field  $\{E_j\}$ , subject to proper normalization, can be presented as a sequence of values  $+1$  and  $-1$ . Since all such sequences of length  $M$  form a mathematical object known as a Galois field  $\text{GF}(2^M)$ , the problem of selective excitation can be linked to the number theory problem of finding sequences of numbers  $+1$  and  $-1$  with minimal autocorrelation. Indeed, for every given Raman shift  $\Omega_R^{j_0} \equiv j_0\Delta\Omega_N$ , the excitation efficiency is determined by  $E_{j_0}^{(0)}$  from Eqn (2), i.e. by correlation of  $\{E_j\}$  and  $\{E_{j+j_0}\}$ . When the binary sequence is repeated after  $\Omega_R^{j_0}$ ,  $E_j^{(0)}$  would have a maximum at  $j = j_0$ . The use of a minimal autocorrelation sequence to modulate the phase, however, ensures that the excitation at nearby frequencies is suppressed.<sup>[15]</sup>

Following the considerations above, the phase mask across the pump-Stokes part of the spectrum is built as follows (see the diagrams in Fig. 1). We first assign the minimal ( $\Omega_{\text{min}}^{\text{PS}}$ ) and maximal ( $\Omega_{\text{max}}^{\text{PS}}$ ) wavenumbers of the pump-Stokes band and compare its bandwidth ( $\Delta\Omega^{\text{PS}} \equiv \Omega_{\text{max}}^{\text{PS}} - \Omega_{\text{min}}^{\text{PS}}$ ) with  $2\Omega_R$ , where  $\Omega_R$  is the selected wavenumber. Here we assume that the pump-Stokes bandwidth  $\Delta\Omega^{\text{PS}}$  exceeds  $\Omega_R$ , i.e. the transition can be excited impulsively. If  $\Delta\Omega^{\text{PS}} < 2\Omega_R$ , as shown in Fig. 1(a), the chosen pseudorandom sequence is stretched over a  $(\Delta\Omega^{\text{PS}} - \Omega_R)$ -wide interval, from  $\Omega_{\text{max}}^{\text{PS}}$  down to  $\Omega_{\text{min}}^{\text{PS}} + \Omega_R$ , and then repeated between  $\Omega_{\text{max}}^{\text{PS}} - \Omega_R$  and  $\Omega_{\text{min}}^{\text{PS}}$ , with translational symmetry relative to the first interval. The interval between  $\Omega_{\text{max}}^{\text{PS}} - \Omega_R$  and  $\Omega_{\text{min}}^{\text{PS}} + \Omega_R$ , which does not contribute toward excitation at  $\Omega_R$ , is filled with a high-frequency random binary phase to suppress the background contribution from this part of the spectrum. If  $\Delta\Omega^{\text{PS}} \geq 2\Omega_R$  (Fig. 1(b)), the Galois sequence is stretched over  $\Omega_R$  and encoded from  $\Omega_{\text{max}}^{\text{PS}}$  to  $\Omega_{\text{max}}^{\text{PS}} - 2\Omega_R$ , and then from  $\Omega_{\text{max}}^{\text{PS}} - 2\Omega_R$  down to  $\Omega_{\text{max}}^{\text{PS}} - \Omega_R$ . The leftover SLM pixels are again filled with a high-frequency random binary phase. In principle, one can put in as many sequence copies as can fit in  $\Delta\Omega^{\text{PS}}$ , i.e. more than 2. The extra copies, however, will contribute to higher harmonics of  $\Omega_R$  as well. Finally, it is worthwhile to note here that Galois sequences are best suited for shaping of flat-top laser spectra. Their minimal autocorrelation property implies equally weighted contribution from every term in a sequence, which is not quite the case for



**Figure 2.** Phase and polarization shaping for multimode and selective single-beam CARS measurements. (a) Polarization mask encoded onto the laser spectrum, shown on the background by the gray line; (b) phase mask for multimode CARS measurements, when all Raman modes within the laser bandwidth are excited; (c and d) pseudorandom phase masks used for selective single-beam CARS from  $O_2$  ( $1550\text{ cm}^{-1}$ ) and  $N_2$  ( $2330\text{ cm}^{-1}$ ), respectively.

the spectrum provided by our laser source. In practice, it results in inferior background suppression when compared to the optimal case.

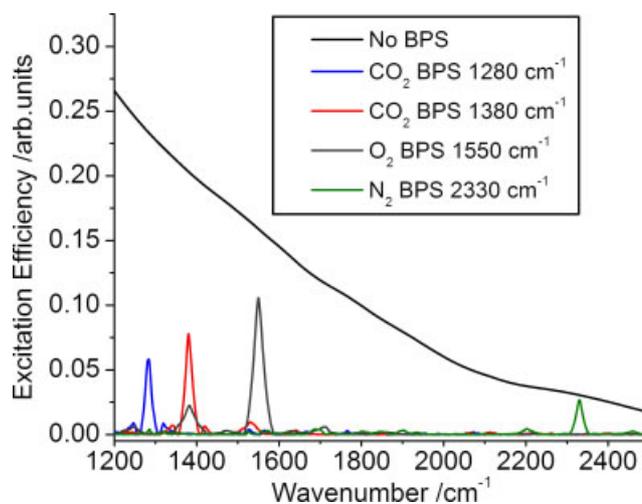
To retrieve CARS spectra, we use a polarization shaping technique.<sup>[6,9]</sup> The polarization of a narrow band on the blue side of the laser spectrum (polarization  $P_x$  in Fig. 2(a), four SLM pixels wide) is rotated by  $90^\circ$  relative to the remaining spectrum. The polarizer in the acquisition arm is also set along this polarization. Only CARS photons with polarization  $P_x$  are detected. The intense  $P_y$ -polarized signal, overwhelmed by the nonresonant background produced by the pump-Stokes component and having poor spectral resolution, is rejected. We also encode a  $\pi$ -phase step across the  $P_x$ -polarized band when acquiring multimode CARS spectra, as shown in Fig. 2(b). The  $\pi$  step is used to minimize the time overlap between the  $P_y$ -polarized pump-Stokes and  $P_x$ -polarized probe parts, mitigating the contribution due to the instantaneous electronic response.

Two examples of selective-excitation phase masks, based on a 37-bit Galois sequence, are shown in Fig. 2(c) and (d). The phase mask in Fig. 2(c) is designed to excite the  $O_2$  vibrational mode at  $\sim 1550\text{ cm}^{-1}$ . For the given experimental parameters, the condition  $\Delta\Omega^{PS} \geq 2\Omega_R$  is fulfilled; therefore, the Galois binary sequence is stretched over  $1550\text{ cm}^{-1}$ , and its two copies are stacked together next to the probe band. The pseudorandom phase mask in Fig. 2(d) targets the  $N_2$  Raman transition at  $\sim 2330\text{ cm}^{-1}$ . Here  $\Delta\Omega^{PS} < 2\Omega_R$  and the two sequence copies are separated by a random binary modulation.

Using this method, phases for selective excitation of the two Fermi dyads of  $CO_2$ , and the Raman modes of  $O_2$  and  $N_2$  were designed. The normalized excitation efficiency spectra  $\eta(\Omega_R)$ ,

$$\eta(\Omega_R) \equiv |E^{(0)}(\Omega_R)/E^{(0)}(0)|^2 \quad (4)$$

for each of the phases as well as for zero phase, which corresponds to a transform limited (TL) pulse, are shown in Fig. 3. From the figure it is clear that BPS is used most effectively when the condition  $\Delta\Omega^{PS} < 2\Omega_R$  is fulfilled. When  $\Delta\Omega^{PS} \geq 2\Omega_R$ , BPS eliminates high-harmonic contributions at the expense of the inferior excitation strength. Raman-shift-dependent excitation efficiencies, both due to the limited laser bandwidth and spectral phase shaping, contribute toward the strength of Raman peaks observed in CARS spectra. In principle, such dependences might

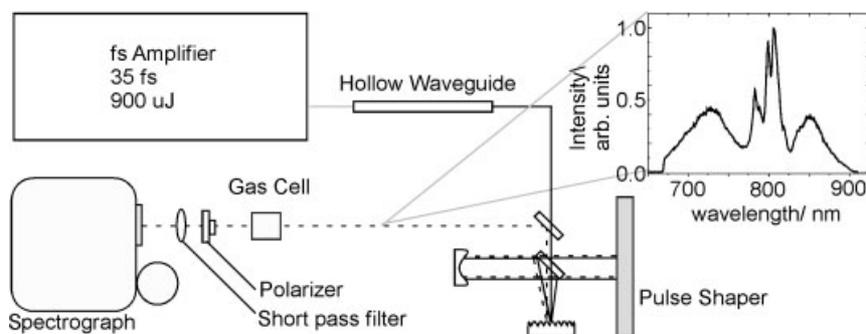


**Figure 3.** Calculated excitation spectra  $\eta(\Omega_R)$  for a transform limited pulse (no phase modulation) and waveforms, produced by pseudorandom binary phase shaping for selective excitation at  $1280$ ,  $1380$ ,  $1550$ , and  $2330\text{ cm}^{-1}$ .

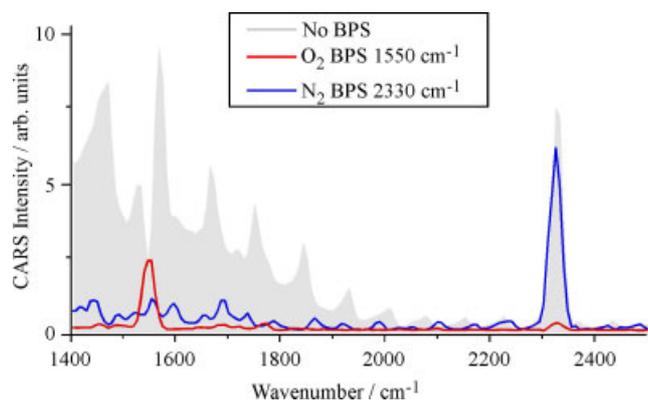
be accounted for experimentally by the normalization of the CARS signal on the purely nonresonant response from a reference sample. To predict the measured CARS spectra or use those to retrieve relative concentrations of contributing species, however, one also needs to account for the timing between the pump-Stokes and probe fields, Raman cross-sections of transitions being examined, and their coherence dephasing rates. This is currently under development, along with other possible methods to perform selective excitation in single-beam CARS.

## Experimental Setup

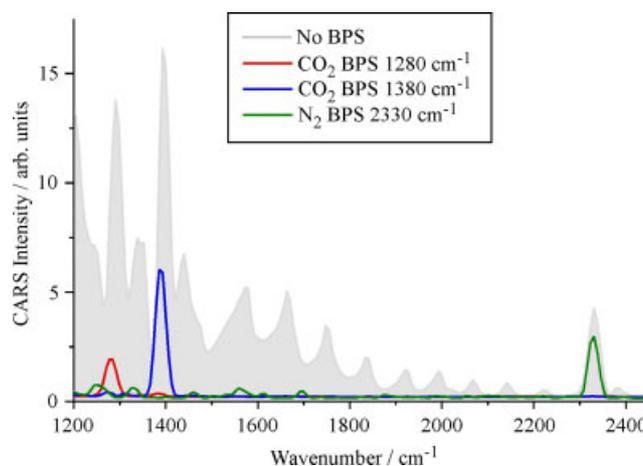
The experiments were performed with a system based on a Ti:sapphire regenerative amplifier (Legend, Coherent Inc.) (Fig. 4). A pulse shaper (not shown) was installed between the oscillator (Micra, Coherent Inc.) and the amplifier to remove high-order phase distortion of laser pulses at the regenerative-amplifier output. The laser spectrum was then broadened through self-phase modulation in a hollow waveguide (HWG),<sup>[18]</sup> constructed from a 39-cm-long glass capillary with a core diameter of  $\sim 300\text{ }\mu\text{m}$  and filled with argon at  $\sim 2$  bar. The HWG output bandwidth was optimized by varying the input power, pulse chirp, and argon pressure. The typical spectrum of a pulse reaching the sampled volume is shown in the inset of Fig. 1. The corresponding TL pulse duration is  $\sim 7$  fs. Phase distortions of the pulse at the sample (primarily linear chirp of  $\sim 2000\text{ fs}^2$ ) were corrected via multiphoton intrapulse interference phase scan (MIIPS),<sup>[19]</sup> performed with a 4f pulse shaper located after the HWG. The same shaper was used for polarization and phase shaping as discussed below. It had a dual-mask 640-pixel spatial light modulator (CRI SLM-640-D) at the Fourier plane, with the polarizer removed. The beam of shaped pulses was focused in ambient air or a gas pressure cell using a curved mirror of 75 cm focal length. A concave metallic mirror with 25 cm focal length was used for imaging of the  $CO_2$  jet. The generated CARS signal was separated from the input field using a 650-nm short-pass filter (Omega Optics) and a calcite polarizing cube (Newport), with the transmission axis set perpendicular to the polarization of the excitation photons. The filtered CARS photons were either focused into a high-resolution



**Figure 4.** Schematic diagram of single-beam CARS experimental setup. SLM, spatial light modulator. Inset: a typical pulse spectrum at the sample.



**Figure 5.** Selective single-beam CARS from  $O_2$  and  $N_2$  vibrations in ambient air.



**Figure 6.** Selective single-beam CARS of a 1 : 1  $N_2/CO_2$  mixture at 1 atm pressure.

spectrograph with a liquid-nitrogen (LN) cooled CCD camera or fiber-coupled into a low-resolution Ocean Optics QE-65000 spectrometer. For imaging experiment, we used two motorized translation stages to shift the nozzle in the focal plane of the laser beam. Spectrally integrated CARS signal over  $1460\text{ cm}^{-1}$  was recorded as a function of the nozzle position.

## Results and Discussion

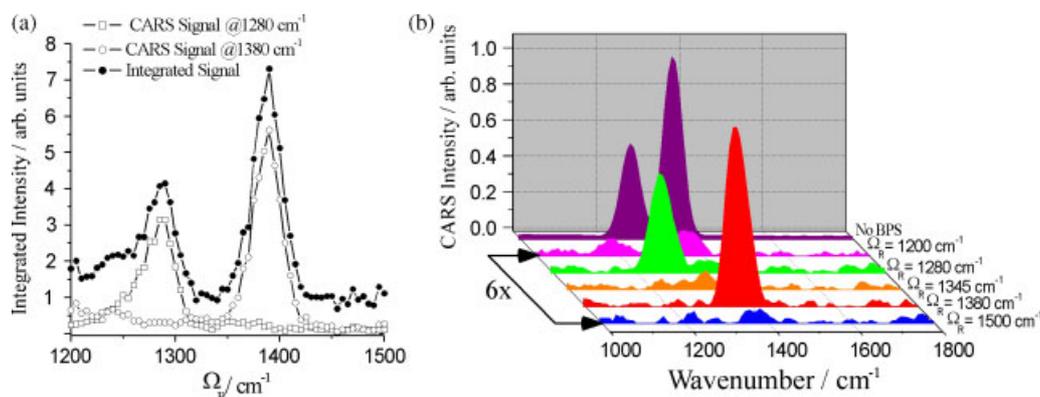
Selective excitation via BPS was examined with several different gases. Initial experiments were performed with ambient air, whose CARS spectrum is expected to have two strong Raman lines corresponding to vibrations of  $O_2$  ( $\sim 1550\text{ cm}^{-1}$ ) and  $N_2$  ( $\sim 2330\text{ cm}^{-1}$ ) molecules. The experimental multimode CARS spectrum (gray shadow in Fig. 5) indeed features a pronounced  $N_2$  line. The  $O_2$  line, however, is hidden by the remaining nonresonant contribution that rises at low wavenumbers. Selective excitation at  $1550\text{ cm}^{-1}$ , using the phase mask from Fig. 2, mitigates the interfering background and makes the  $O_2$  line obvious. The other pseudorandom phase mask highlights the  $N_2$  vibrational mode. The slight offset of the spectra from zero is due to the electronic dark current of the LN-cooled CCD used for detection.

Single-beam CARS measurements with a 1 : 1  $N_2/CO_2$  mixture in the pressure cell showed similar results. In the multimode CARS spectrum, the nonresonant background due to the instantaneous electronic response interferes with the two  $CO_2$  signatures (Fig. 6). The designed binary phase masks allow the excitation of all three Raman lines, including the  $N_2$  line and  $CO_2$  Fermi dyads at  $\sim 1280$

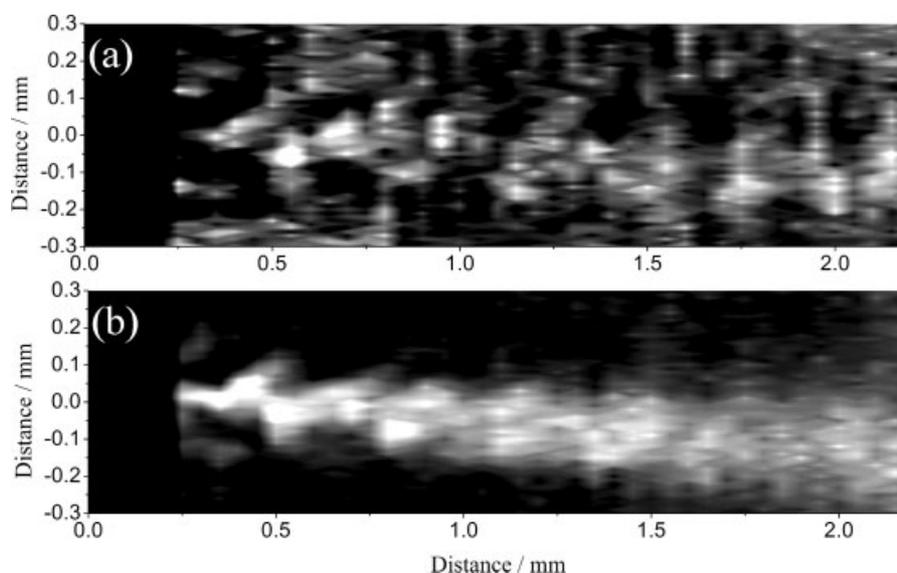
and  $\sim 1380\text{ cm}^{-1}$ , independently. They also strongly suppress the nonresonant background.

The excitation selectivity contrast can be inferred from Fig. 7(a), where the CARS signal intensities at  $1280\text{ cm}^{-1}$ ,  $1380\text{ cm}^{-1}$  and over the entire spectral region ( $625\text{--}2125\text{ cm}^{-1}$ ) from pure  $CO_2$  gas at 1 atm are plotted as a function of the design parameter  $\Omega_R$ . Several representative CARS spectra, acquired with Ocean Optics QE-65000 spectrometer while scanning  $\Omega_R$ , are shown in Fig. 7(b). When the  $1280\text{ cm}^{-1}$  line is selectively excited, the ratio of CARS intensities between the  $1280$  and  $1380\text{ cm}^{-1}$  lines is 10 : 1. For selective excitation of the  $1380\text{ cm}^{-1}$   $CO_2$  line, the ratio between the  $1280$  and  $1380\text{ cm}^{-1}$  lines is 1 : 24. When the CARS signal is not resolved spectrally, the contrast is limited primarily by the cumulative nonresonant contribution reaching the detector.

To emphasize the utility of selective BPS, we imaged a jet of  $CO_2$  gas, flowing out a narrow rectangular nozzle, with TL and shaped pulses. In both cases, a  $0.6 \times 2.2\text{ mm}$  region near the tip of the nozzle was scanned using  $0.01\text{-mm}$  and  $0.05\text{-mm}$  step sizes along vertical and horizontal axes, respectively. The spectrally integrated CARS signal from  $1060$  to  $2520\text{ cm}^{-1}$  was recorded at each position in the scan. The image obtained with TL pulses (Fig. 8(a)) exhibits poor chemical contrast, which can be improved by spectral filtering of the CARS signal corresponding to the  $CO_2$  lines or by post-processing of CARS spectra if those are available. Note that the CARS spectra over the observed range featured  $N_2$  and  $O_2$  lines from ambient air as well as comparable nonresonant contribution



**Figure 7.** Selective single-beam CARS of pure  $\text{CO}_2$  at 1 atm. The target Raman shift  $\Omega_R$  of the pseudorandom binary phase is tuned through the two resonances with  $\text{CO}_2$  Fermi dyads at  $\sim 1280$  and  $\sim 1380$   $\text{cm}^{-1}$ . (a) CARS signal intensities at  $1280$   $\text{cm}^{-1}$ ,  $1380$   $\text{cm}^{-1}$ , and integrated over  $625$ – $2125$   $\text{cm}^{-1}$  as a function of  $\Omega_R$ . (b) Experimental CARS spectra acquired for  $\Omega_R$  equal to  $1200$ ,  $1280$ ,  $1330$ ,  $1380$ , and  $1500$   $\text{cm}^{-1}$ . The multimode, single-beam CARS spectrum of  $\text{CO}_2$  (no BPS) is shown as a reference. The other CARS spectra are scaled in intensity by a factor of 6.



**Figure 8.** Imaging of a  $\text{CO}_2$  gas jet with (a) no BPS and (b) BPS excitation at  $1280$   $\text{cm}^{-1}$ .

at lower wavenumbers (longer wavelengths). Selective excitation, implemented in Fig. 8(b) for the  $1280$   $\text{cm}^{-1}$  Raman transition in  $\text{CO}_2$ , virtually eliminates the need for signal post-processing, favors single-channel detection, and allows straightforward tuning between different Raman resonances. The image in Fig. 8(b) demonstrates excellent chemical contrast and reveals interesting dynamics of the turbulent  $\text{CO}_2$  flow. In particular, the intensity modulation seen in the  $\text{CO}_2$  flow is reproducible from image to image and is deemed to be characteristic of the imaged jet.

## Conclusions

We have extended the pseudorandom BPS technique, introduced elsewhere, to selective excitation of high-wavenumber molecular vibrational modes in the gas phase. In particular, we have used it to address Raman transitions of  $\text{O}_2$  and  $\text{N}_2$  in ambient air as well as  $\text{CO}_2$  Fermi dyads in a  $1:1$   $\text{N}_2/\text{CO}_2$  mixture and pure  $\text{CO}_2$  gas at atmospheric pressure. We have shown that pulse phase shaping using pseudorandom BPS allows high contrast selectivity and

efficient nonresonant background suppression in single-beam CARS measurements, enabling high-contrast spectroscopy and imaging.

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