

CEM 991: Quantum Chemistry and Statistical Thermodynamics I (Fall 2021)

Course Outline

Chapter in a Textbook[#]

1. The Origins of Quantum Mechanics	
1.1. Overview of classical mechanics and electrodynamics	4,14,23
1.2. The old quantum theory, inadequacy of classical physics	1
1.3. Uncertainty principle, limitations on experiment, wave-packet formalism	1,2
2. The Schrödinger Wave Equation	
2.1. Time-dependent and time-independent Schrödinger equations, position and momentum operators	3
2.2. Interpretation of the wave function, expectation value, Ehrenfest's theorem	3
2.3. Boundary and continuity conditions, bound and unbound states	3
2.4. One-dimensional square well potential, parity	5,6
3. Mathematical Foundations of Quantum Mechanics	
3.1. Linear, metric, unitary, and Hilbert spaces	9
3.2. Linear, adjoint, Hermitian, and self-adjoint operators, eigenvalue problems, operator spectra	3,4,9,10
3.3. Operators in quantum mechanics, Dirac's notation	3,4,9,10
3.4. Projection operators, orthonormal, closed, and complete sets, basis	4,9,10
3.5. Resolution of identity, spectral theorems, Dirac's δ -distribution, orthonormalization of eigenstates, the closure property for operators having discrete and continuous spectra	4,9,10,Appendix
3.6. Commutators and simultaneous observables	3,10
3.7. Postulates of quantum mechanics	4,14
3.8. General solution of the Schrödinger equation	3,15
3.9. Heisenberg's uncertainty principle revisited	10
4. Analytic Solutions of the Schrödinger Equation	
4.1. Linear harmonic oscillator, generating functions for orthogonal polynomials	5
4.2. Central potentials, angular momentum, spherical harmonics, two-body problem, the hydrogen atom	11,12,15
5. Matrix Formulation of Quantum Mechanics	
5.1. Matrix representation of linear operators and quantum states, change of basis, representations	9,10,15
5.2. Schrödinger and Heisenberg pictures, quantization of classical mechanics	14
5.3. Matrix theory of the harmonic oscillator, creation and annihilation operators	10
6. Quantum Theory of Angular Momentum (time permitting, optional)	
6.1. Commutation relations, the SO(3) group and its representations, the Casimir operators	11,16,17
6.2. Eigenvalue problem, angular momentum matrices, spin	11,16
6.3. Direct product representations, the Clebsch-Gordan coefficients, coupling angular momenta	17
7. Approximate Methods (time permitting, optional)	
7.1. Stationary (bound-state) perturbation theory	18
7.2. Time-dependent perturbation theory	19
7.3. Variational approach	8,18

[#] The textbook provides a general framework for the course, and useful information about the material taught during lectures can be found in it, but is not required reading. All lectures, homework assignments, and midterm and final exams will be based on the lecture notes and handouts provided to the students by the instructor.