

$$2) \quad P = \int_x^{\infty} e^{-x^2} dx \Rightarrow x = 0.5 / 0.098 = 5.1$$

$$= 8.97 \times 10^{-7}$$

2) (a) Bipolar pulses are "neutral" with respect to current flow through a circuit. ~~With~~ Unipolar pulses require a net flow of current through the circuit whence they pass.

(b) The "zero crossing" point of a series of bipolar pulses is constant with respect to the time of origin of the pulse.

3) (a) negative high voltage bases produce the output pulse at ground and allow "DC" coupling of the pulse into subsequent electronic circuits

(b) positive high voltage puts the photocathode at ground potential whereas negative HV puts the photocathode at negative high voltage and a ^{large static} charge can develop across the glass surface on which the photocathode is plated (which can be dangerous if not properly designed).

4) (a) electric field $E = \frac{960 \text{ V}}{25 \text{ cm}} = 36 \text{ V/cm}$, $\mu = 2 \times 10^4 \frac{\text{cm}^2}{\text{Vs}} \frac{960 \text{ Torr}}{200 \text{ Torr}} = 7.6 \times 10^4 \frac{\text{cm}^2}{\text{Vs}}$

electron velocity $v = \mu E = 7.6 \times 10^4 \frac{\text{cm}^2}{\text{Vs}} \times \frac{36 \text{ V}}{\text{cm}} = 2.74 \times 10^6 \text{ cm/s}$

(non relativistic) $t = \frac{x}{v} = \frac{25 \text{ cm}}{2} / 2.74 \times 10^6 \text{ cm/s} = 4.6 \times 10^{-6} \text{ sec}$

(b) $\sigma_x = 300 \mu\text{m}$, $x = vt \rightarrow \frac{\sigma_x}{x} = \frac{\sigma_t}{t}$

(continue)

4 (b) con't $\frac{\sigma_x}{x} = \frac{\sigma_z}{z} \rightarrow \frac{350 \times 10^{-6} \text{ m}}{12.5 \times 10^{-2} \text{ m}} = \frac{\sigma_z}{4.6 \times 10^{-6} \text{ s}}$

Total ~~noise~~ $\sigma_z = 0.0024 \times 4.6 \times 10^{-6} \text{ s} = 1.1 \times 10^{-8} \text{ s}$ or 11 ns

(c) σ_z^{DRIFT} from CFD against scint $\sigma_z^{\text{SCINT}} = 0.25 \text{ ns}$

$$(\sigma_z^{\text{TOTAL}})^2 = (\sigma_z^{\text{DRIFT}})^2 + (\sigma_z^{\text{SCINT}})^2$$

$$\sigma_z^{\text{DRIFT}} = \left[(\sigma_z^{\text{TOTAL}})^2 - (\sigma_z^{\text{SCINT}})^2 \right]^{1/2} = \left[11^2 - 0.25^2 \right]^{1/2} \approx 11$$

in CFD $\sigma_z = \text{rise time} / \sqrt{2} = 11 \text{ ns} = \frac{100 \text{ ns}}{\sqrt{2}} \rightarrow \text{S/N} = \frac{100}{11} = 9.09$

so S/N = 9.09, noise $\approx \frac{1}{9.09} \approx \frac{1.00 \text{ V}}{9.09} = 0.11 \text{ V}$ (pretty easy to get this)

(d) $\ln M = \frac{V}{\ln(b/a)} \frac{\ln 2}{\Delta V} \left[\ln \left(\frac{V}{K \rho a \ln(b/a)} \right) \right]$

$a = 25 \mu\text{m}/2$
 $b = 10. \text{ mm}/2$
 $\rho = 200 \text{ torr}$
 $P\text{-}1\phi \Delta V = 23.6 \text{ V}$ Table 6.1
 $K = 4.8 \times 10^4 \frac{\text{V}}{\text{cm atm}}$

$$\ln M = \frac{1000 \text{ V}}{\ln \left(\frac{10^{-2} \text{ m}}{25 \times 10^{-6} \text{ m}} \right)} \frac{\ln 2}{23.6 \text{ V}} \left[\ln \frac{1000 \text{ V}}{4.8 \times 10^4 \frac{\text{V}}{\text{cm atm}} \frac{25 \times 10^{-4} \text{ m}}{2} \times 10^2 \ln \left(\frac{200}{760} \right) \ln \left(\frac{10^{-2}}{25 \times 10^{-6}} \right)} \right]$$

$\ln M = 4.384 \ln [4.393] = 9.88 \rightarrow M = 19,500$

(e) $N_{IP} (\text{in Gas}) = \frac{15 \times 10^6 \text{ eV}}{26 \text{ eV/IP}}$ Table 6.2 = 5.77×10^5

$N_{\text{wire}} = M \times N_{IP} = 19,500 \times 5.77 \times 10^5 = 1.13 \times 10^{10}$ (wow)

from lecture $\left(\frac{\sigma_Q}{Q} \right)^2 = \left(\frac{F}{N_{IP}} \right) + \frac{1}{N_{IP}} \rightarrow \left(\frac{\sigma_Q}{Q} \right)^2 = \frac{1.21}{5.77 \times 10^5} = 2.1 \times 10^{-6}$

(f) The signal is created by the motion of the cations away from the central wire. The induced signal is read out on the σ stripes.

$$\frac{\sigma_Q}{Q} = 1.44 \times 10^{-3}$$

$$R = 2.354 \left(\frac{\sigma_Q}{Q} \right) = 3.41 \times 10^{-3}$$

Beverington

APPENDIX C

GRAPHS AND TABLES

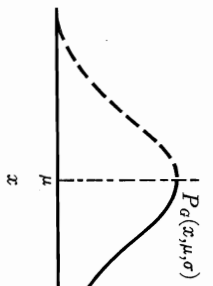


Table C-1 Gaussian probability distribution. The Gaussian or normal error distribution $P_G(x, \mu, \sigma)$ vs. $z = |x - \mu|/\sigma$

C-1 GAUSSIAN PROBABILITY DISTRIBUTION

The probability function $P_G(x, \mu, \sigma)$ for the Gaussian or normal error distribution is given by

$$P_G(x, \mu, \sigma) = \frac{1}{\sigma \sqrt{2\pi}} \exp \left[-\frac{1}{2} \left(\frac{x - \mu}{\sigma} \right)^2 \right]$$

If measurements of a quantity x are distributed in this manner around a mean μ with a standard deviation σ , the probability $dP_G(x, \mu, \sigma)$ for observing a value of x , within an infinitesimally small interval dx , in a random sample measurement is given by

$$dP_G(x, \mu, \sigma) = P_G(x, \mu, \sigma) dx$$

Values of the probability function $P_G(x, \mu, \sigma)$ are tabulated in Table C-1 as a function of the dimensionless deviation

$$z = |x - \mu|/\sigma$$

for z ranging from 0.0 to 3.0 in increments of 0.01 and up to 5.9 in increments of 0.1. These values were calculated with the sub-routine GAUSS of Program 3-4. This function is graphed on a semilogarithmic scale as a function of z in Figure C-1.

The function which is tabulated and graphed is $P_G(z, 0, 1)$ which gives the probability that $x = \mu \pm z\sigma$. It is the curve of Figure 3-5 tabulated only for positive values of z as indicated.

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.39894	.39892	.39886	.39876	.39862	.39844	.39822	.39797	.39767	.39733
0.1	.39695	.39654	.39608	.39559	.39505	.39448	.39387	.39325	.39255	.39181
0.2	.39104	.39024	.38940	.38853	.38762	.38667	.38568	.38466	.38361	.38251
0.3	.38139	.38023	.37903	.37780	.37654	.37524	.37391	.37255	.37115	.36973
0.4	.36827	.36678	.36526	.36371	.36213	.36053	.35889	.35723	.35555	.35381
0.5	.35207	.35029	.34849	.34667	.34482	.34294	.34105	.33912	.33718	.33521
0.6	.33322	.33121	.32918	.32713	.32506	.32297	.32086	.31874	.31659	.31443
0.7	.31225	.31006	.30785	.30563	.30339	.30114	.29887	.29659	.29431	.29200
0.8	.28969	.28737	.28504	.28269	.28034	.27799	.27562	.27324	.27086	.26848
0.9	.26609	.26369	.26129	.25888	.25647	.25406	.25164	.24923	.24681	.24439
1.0	.24187	.23955	.23713	.23471	.23230	.22988	.22747	.22506	.22266	.22025
1.1	.21785	.21546	.21307	.21069	.20831	.20594	.20357	.20122	.19887	.19652
1.2	.19419	.19186	.18955	.18724	.18493	.18265	.18038	.17812	.17587	.17362
1.3	.17137	.16915	.16694	.16475	.16259	.16042	.15827	.15612	.15397	.15182
1.4	.14973	.14764	.14557	.14351	.14147	.13942	.13738	.13533	.13329	.13124
1.5	.12962	.12758	.12557	.12357	.12158	.11962	.11767	.11572	.11378	.11184
1.6	.11032	.10916	.10721	.10568	.10397	.10227	.10059	.09893	.09729	.09567
1.7	.09406	.09247	.09030	.08834	.08629	.08428	.08230	.08034	.07841	.07650
1.8	.07486	.07255	.07061	.06895	.06734	.06577	.06422	.06269	.06118	.05968
1.9	.06562	.06439	.06316	.06196	.06077	.05960	.05845	.05731	.05619	.05509
2.0	.05400	.05293	.05187	.05083	.04981	.04880	.04781	.04683	.04587	.04492
2.1	.04309	.04217	.04129	.04041	.03956	.03871	.03788	.03707	.03627	.03547
2.2	.03548	.03471	.03395	.03320	.03247	.03175	.03104	.03034	.02966	.02899
2.3	.02833	.02769	.02705	.02643	.02582	.02522	.02464	.02406	.02350	.02294
2.4	.02240	.02187	.02135	.02083	.02033	.01984	.01936	.01889	.01843	.01798
2.5	.01753	.01710	.01667	.01626	.01585	.01545	.01506	.01468	.01431	.01394
2.6	.01359	.01324	.01290	.01256	.01224	.01192	.01160	.01130	.01100	.01071
2.7	.01042	.01015	.00987	.00961	.00935	.00910	.00885	.00861	.00837	.00813
2.8	.00792	.00770	.00749	.00728	.00707	.00688	.00668	.00649	.00631	.00613
2.9	.00595	.00578	.00562	.00546	.00530	.00514	.00500	.00485	.00471	.00457
3.0	.0044318	.0032668	.0023841	.0017226	.0012332	.0008479	.00052919	.0003232	.00019866	.0011986
3.5	.000827269	.00061191	.00042479	.00028479	.00019866	.00013953	.00009853	.000067479	.00004479	.00002986
4.0	.00013383	.000089264	.000058945	.000038855	.000024993	.0000163701	.000010414	.0000063701	.0000039615	.0000024993
4.5	.000015984	.000010184	.0000063701	.0000039615	.0000024993	.0000015984	.0000010184	.00000063701	.00000039615	.00000024993
5.0	.0000014868	.00000089730	.00000053614	.00000031716	.00000018575	.0000001102	.00000006183	.00000003514	.0000000201978	.00000001102
5.5	.000000010771	.000000006183	.000000003514	.00000000201978	.000000001102	.0000000006183	.0000000003514	.000000000201978	.0000000001102	.00000000006183