

1 (a) Gain = 8^N , $5^{10} = 9.77 \times 10^6$

(b) one/synode $\frac{\sigma}{N} = \frac{\sqrt{5}}{5} = 0.447$

(c) amplified signal from one e^- $\left(\frac{\sigma}{N}\right)^2 \sim \frac{1}{8-1}$ (Eq 9.4)
 $\sigma_{\text{sig}}/N = \left(\frac{1}{4}\right)^{1/2} = \frac{1}{2}$

(d) amplified signal from $10^4 e^-$'s ... we could imagine that we are taking 10^4 samples (if there is no interaction during cascade) ... thus the error would be reduced by $\frac{1}{\sqrt{10^4}} = \frac{1}{10}$
 $(\sigma_{\text{sig}}/N) = \frac{1}{2} \times \frac{1}{10} = 0.05$

2 (a) $\ln \eta = \frac{V}{\ln(b/a)} \frac{\ln Z}{\Delta V} \left\{ \ln \frac{V}{p a \ln(b/a) K} \right\}$ (eq 6.8)

P-10 $\Delta V = 23.6 \text{ V}$, $K = 4.8 \times 10^4 \text{ V/cm}^2$ Table 6.1

$$\ln \eta = \frac{20000}{\ln(5/0.005)} \frac{\ln Z}{23.6} \left\{ \ln \frac{20000}{1(0.005) \ln(5/0.005) 4.8 \times 10^4} \right\}$$

$\ln \eta = 1.595 \rightarrow \eta = 4.93$

(b) $V = \frac{Q}{C} M = \frac{5.0 \times 10^6 \text{ eV} \times 1.602 \times 10^{-19}}{20 \text{ eV/IP}} \times \frac{4.93}{10^4 \times 10^{-12}} \frac{\text{cm}}{\text{fund}}$

W from Table 6.2

$V = 1.5 \times 10^3 \text{ V}^2/\text{cm}$

3 (a) Resolution (following Eq 4-15 or 12-13)

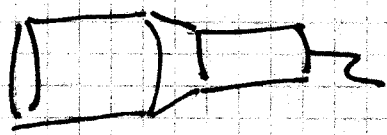
$$\text{Resolution} = 2.354 (FWE)^{1/2} = 2.354 (\phi \cdot \phi 8 [7.68 \text{ eV}] 10^6 \text{ eV})^{1/2}$$

(7) Resolution = 1.8 keV

(b) $Z_{Ge} = 32 < (Z_{Pb} = 82, Z_I = 53)$

(3) thus because photoelectric σ depends on Z^5 or so most counts should be in photopeak for PbI_2

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$$\tau_{elec} = RC = (10^2 \times 10^{-12}) 5\phi$$
$$RC = 5 \times 10^{-9} \text{ sec}$$

\rightarrow $1 \text{ MeV} \times 38 \phi \phi \times \phi 8 \phi \times \phi 2 \phi \times 10^4 = N_0$
 $6 \cdot \phi 8 \times 10^7 = N_0$

$$Q = N_0 e = 6 \phi 8 \times 10^7 \times 1.6 \phi 2 \times 10^{-19} \text{ coul} = 9.74 \times 10^{-12} \text{ coul}$$

(6) $V_R = \frac{Q}{C} = \frac{9.74 \times 10^{-12}}{10^2 \times 10^{-12}} = 9.7 \times 10^{-2} \text{ V}$ limit for large RC

τ electronics is fast compared to $\tau \sim \phi 23 \mu\text{s}$ light

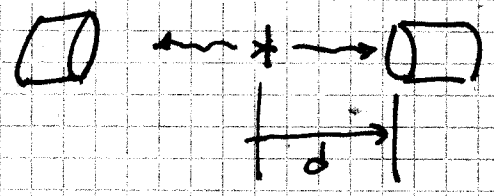
max τ radiation $\sim \frac{10 \text{ cm}}{3 \times 10^8 \text{ cm/sec}} \approx 33 \text{ ns}$

for small time constant $V = \frac{\tau}{\theta} \frac{Q}{C}$ [cf 9.17a]

$$V_R = \left(\frac{\tau_{nat}}{\tau_{elec}} \right)^{-1} \frac{Q}{C} = \frac{0.605 \mu\text{s}}{0.23 \mu\text{s}} (9.7 \times 10^{-2} \text{ V}) = 2.1 \times 10^{-3} \text{ V}$$

(4)

5



$$A_{\text{DB}} = 1\phi \mu\text{Ci} \times 3.7 \times 10^{10} \frac{1\phi}{\text{sec}} \times 1\phi^{-6} \frac{\text{Ci}}{\mu\text{Ci}}$$

$$A_{\text{DB}} = 3.7 \times 10^5 \text{ into } 4\pi$$

(a) photo peak eff. \sim @ 1.1 or 1.3 MeV for ^{60}Co $\sim \phi.3 = \frac{\epsilon}{\text{inst}}$
 fig 10.25

(b) want $R_1 = R_2 = 1\phi^2 / \text{sec} = A \epsilon_{\text{inst}} \epsilon_{\text{geo}} W(\theta)$

if there is no angular correlation ... low rate ignore summing

$$\epsilon_{\text{geo}} = \frac{1\phi^2 / \text{sec}}{3.7 \times 10^5 / \text{sec} (\phi.3)} = 9\phi \times 1\phi^{-4}$$

[eq 4.22] and $\epsilon_{\text{geo}} \sim \frac{\pi a^2}{4\pi d^2} \rightarrow d = \left[\frac{\pi (7.6/2)^2}{4\pi (9\phi \times 1\phi^{-4})} \right]^{1/2} \text{ cm}$

$$d = [4\phi \times 1\phi^3 \text{ cm}^2] = 63. \text{ cm}$$

"separate" by 2d or 126 cm

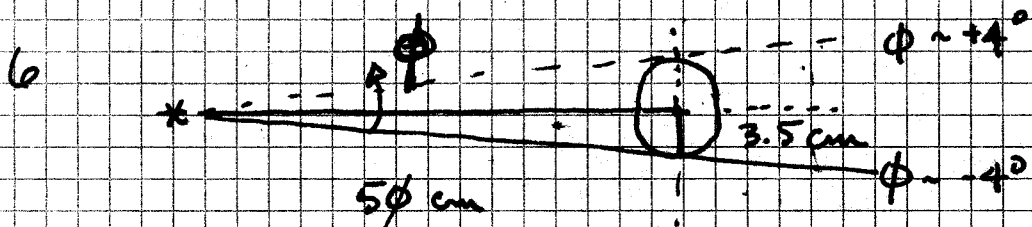
(c) $R_{12} = (A \epsilon_{\text{geo}})(A \epsilon_{\text{geo}}) \neq \epsilon$ [Eq 10.13]

[use total ϵ not photopeak]

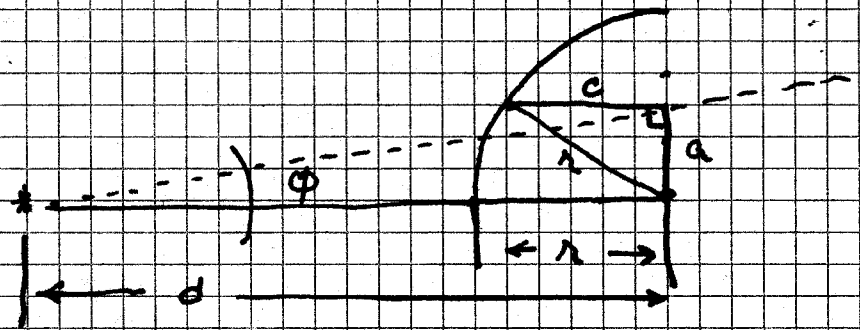
$$R_{12} = \left(3.7 \times 10^5 / \text{sec} \times 9\phi \times 1\phi^{-4} \right)^2 \times 1\phi^{-6} \text{ sec}$$

$$= \left(333 \frac{1}{\text{sec}} \right)^2 \times 1\phi^{-6} \text{ sec} = \phi.44 / \text{sec}$$

[or 1 in 250 is rand]



$$\frac{\phi}{2} \sim \tan^{-1} \left(\frac{3.5}{5\phi} \right) \sim 4^\circ$$



approximate the path across the detector by the "cord" of the circle

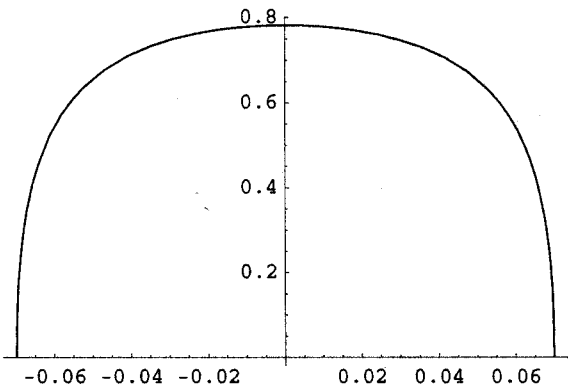
$$c^2 = r^2 - a^2 \quad \tan \phi = \frac{a}{d} \rightarrow c = [r^2 - (d \tan \phi)^2]^{\frac{1}{2}}$$

frac. attenuation = $1 - \frac{I}{I_0} = 1 - e^{-\mu(2c)}$

from NIST website $\mu/\rho = \phi \cdot \phi 4 \phi 8 6 \frac{\text{cm}^2}{\text{g}}$ for Ge @ 2 MeV
 $\rho = 5.323 \text{ g/cm}^3$

GeAttenuation.nb

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In[51]:= Plot[
  {1 - Exp[-0.04086 5.323 + 2 cord[3.5, 50, phi] ]},
  {phi, -phiMax[3.5, 50], phiMax[3.5, 50]}
]
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Out[51]= - Graphics -

7

- should be sensitive to fast neutrons (only)
- Cd sheet absorbs thermal neutrons
- ~~the~~ paraffin $(CH_2)_n$ thermalizes neutrons that pass through the Cd sheet due to high energy
- BF_3 proportional counter absorbs thermal neutrons
Cd gives an ionization pulse $^{10}B + n \rightarrow ^7Li + 4He + Q$
 $\rightarrow ^7Li^* + 4He + Q'$
- pulse height distribution contains little information, only the presence of a neutron reaction when above a noise threshold or AKa , pulses from γ 's

8

$$(a) \text{ deadline per event} = (\text{time to digitize}) + (\text{time to store})$$

$$= 10 \mu s + n(3 \mu s)$$

$$= 10 + 10(3) \mu s / \text{event}$$

$$\tau = 40 \mu s / \text{event}$$

where n is # of words
opposite case to that in text/books

nonparal.

$$(b) R_{\text{obs}} = \frac{R_{\text{TROE}}}{1 + R_{\text{TROE}} \tau} = \frac{2000}{1 + 2000(40 \times 10^{-6})}$$

$$R_{\text{obs}} = 198. / \text{sec}$$

$$\text{fraction dead} = R_{\text{obs}} \tau = 198 \times 40 \times 10^{-6} = 7.9 \times 10^{-3}$$

$$(c) 0.50 = R_{\text{obs}} \tau \rightarrow R_{\text{obs}} = \frac{0.50}{4 \times 10^{-5}} = 12,500 / \text{sec}$$

$$12500 = \frac{R_T}{1 + R_T \tau}$$

$$12500(1 + R_T \tau) = R_T$$

$$12500 + 0.5 R_T = R_T$$

$$12500 = 0.5 R_T$$

$$25000 = R_T$$

[obviously]