

## CHAPTER 5

- 5-1. Frequency dependent noise sources: flicker and environmental noise.  
Frequency independent sources: thermal and shot noise.
- 5-2. (a) Thermal noise.  
(b) Certain types of environmental noise.  
(c) Thermal and shot noise.
- 5-3.  $10^3$  to  $10^5$  Hz and  $10^6$  to  $10^7$  Hz, Environmental noise is at a minimum in these regions  
(see Figure 5-3).
- 5-4. At the high impedance of a glass electrode, shielding is vital to minimize induced currents from power lines which can be amplified and can disturb the output.
- 5-5. (a) High-pass filters are used to remove low frequency flicker noise from higher frequency analytical signals.  
(b) Low-pass filters are used to remove high frequency noise from dc analytical signals.
- 5-6. We estimate the maximum and the minimum in the recorded signal ( $0.9 \times 10^{-15}$  A) to be  $1.5 \times 10^{-15}$  and  $0.4 \times 10^{-15}$  A. The standard deviation of the signal is estimated to be one-fifth of the difference or  $0.22 \times 10^{-15}$  A. Thus,

$$\frac{S}{N} = \frac{0.9 \times 10^{-15} \text{ A}}{0.22 \times 10^{-15} \text{ A}} = 4$$

5-7. (a)

	A	B	C
1			
2	<b>Problem 5-7</b>		
3		<b>Weighings</b>	
4		1.003	
5		1.004	
6		1.001	
7		1.000	
8		1.005	
9		0.999	
10		1.001	
11		1.006	
12		1.007	
13	<b>Mean</b>	1.003	
14	<b>Std. Dev.</b>	0.002804	
15	<b>RSD</b>	0.002796	
16	<b>S/N</b>	357.6933	
17			
18	<b>Spreadsheet Documentation</b>		
19	Cell B13=AVERAGE(B4:B12)		
20	Cell B14=STDEV(B4:B12)		
21	Cell B15=B14/B13		
22	Cell B16=1/B15		

Hence,  $S/N = 358$  for these 9 measurements

(b) 
$$\frac{S}{N} = \frac{S_n}{N_n} \sqrt{n} \quad (\text{Equation 5-11}). \quad \text{For the nine measurements,}$$

$$358 = \frac{S_n}{N_n} \sqrt{9}$$

For the  $S/N$  to be 500 requires  $n_x$  measurements. That is,

$$500 = \frac{S_n}{N_n} \sqrt{n_x}$$

Dividing the second equation by the first gives, after squaring and rearranging,

$$n_x = \left( \frac{500}{358} \times 3 \right)^2 = 17.6 \quad \text{or 18 measurements}$$

5-8. (a)

	A	B	C
1			
2	<b>Problem 5-8</b>		
3		<b>Voltages</b>	
4		1.37	
5		1.84	
6		1.35	
7		1.47	
8		1.10	
9		1.73	
10		1.54	
11		1.08	
12	<b>Mean</b>	1.435	
13	<b>Std. Dev.</b>	0.270713	
14	<b>RSD</b>	0.18865	
15	<b>S/N</b>	5.30081	
16			
17	<b>Spreadsheet Documentation</b>		
18	Cell B12=AVERAGE(B4:B11)		
19	Cell B13=STDEV(B4:B11)		
20	Cell B14=B13/B12		
21	Cell B15=1/B14		

Thus  $S/N = 5.3$

(b) Proceeding as in Solution 5-7, we obtain

$$n_x = \left( \frac{10}{5.3} \times \sqrt{8} \right) = 28.5 \quad \text{or 29 measurements}$$

$$5-9. \quad \bar{v}_{\text{rms}} = \sqrt{4kTR\Delta f} = \sqrt{4 \times 1.38 \times 10^{-23} \times 298 \times 1 \times 10^6 \times 1 \times 10^6} = 1.28 \times 10^{-4} \text{ V}$$

$\bar{v}_{\text{rms}} \propto \sqrt{\Delta f}$  So reducing  $\Delta f$  from 1 MHz to 100 Hz, means a reduction by a factor of

$10^6/10^2 = 10^4$  which leads to a reduction in  $\bar{v}_{\text{rms}}$  of a factor of  $\sqrt{10^4} = 100$ .

5-10. To increase the  $S/N$  by a factor of 10 requires  $10^2$  more measurements. So  $n = 100$ .

5-11. The middle spectrum  $S/N$  is improved by a factor of  $\sqrt{50} = 7.1$  over the top spectrum.

The bottom spectrum  $S/N$  is improved by a factor of  $\sqrt{200} = 14.1$  over the top spectrum.

The bottom spectrum is the result of  $200/50 = 4$  times as many scans so the  $S/N$  should be improved by a factor of  $\sqrt{4} = 2$  over the middle spectrum

- 5-12. The magnitudes of the signals and the noise in the spectra in Figure 5-15 may be estimated directly from the plots. The results from our estimates are given in the table below. Baselines for spectra  $A$  and  $D$  are taken from the flat regions on the right side of the figure. Noise is calculated from one-fifth of the peak-to-peak excursions of the signal.

	$A_{255}$	$A_{425}$	$A_b(\text{peak})$	$A_b(\text{valley})$	$A_b(\text{mean})$
Spectrum $A$	0.550	0.580	0.080	-0.082	0.001
Spectrum $D$	1.125	1.150	0.620	0.581	0.600

  

	$S_{255}$	$S_{425}$	$N = [A_b(\text{peak}) - A_b(\text{valley})]/5$	$(S/N)_{255}$	$(S/N)_{425}$
Spectrum $A$	0.549	0.579	0.0324	17	18
Spectrum $D$	0.525	0.550	0.0078	67	70

Note that the difference in  $S/N$  for the two peaks is due only to the difference in the peak heights.

So, at 255 nm,  $(S/N)_D = 67/17(S/N)_A = 3.9(S/N)_A$ ; at 425 nm,  $(S/N)_D = 70/18(S/N)_A = 3.9(S/N)_A$