

## Nuclear Chemistry Cumulative Examination

**Wednesday, 27 February 2013**

Write your answers to the following questions *in the order listed*. Make sure that the answers are well-organized and self-explanatory. The total number of points on this exam is 50.

1. (2 point each) Give concise and accurate answers to the following questions:

- (a) What is the key feature of two nuclides that are said to have the same “isospin projection?”
- (b) What is the key feature of two nuclides that are said to be “isomers?”
- (c) What is the relationship between the partial half-life and (full) half-life of a radionuclide?
- (d) Write a COMPLETELY balanced equation for the  $\beta^+$  decay of the nuclide  $^{22}\text{Na}$  ( $Z=11$ , a nuisance activity with a half life of 2.60 years that is often produced when accelerated beams strike aluminum).
- (e) The *lepton number* is conserved in nuclear decay. What is a lepton in this context?

2. (5 points each) The  $^{132}\text{Sn}$  nuclide is something of a special nuclide because it is strongly produced in the fission of uranium, it is a so-called doubly-magic nucleus, and it decays with a half-life of 39.7s. The ground state intrinsic spin and parity of  $^{132}\text{Sn}$  is  $0^+$  and it decays with a Q-value of 3119 keV to the radioactive nucleus  $^{132}\text{Sb}$  that has a ground-state intrinsic spin/parity of  $4^+$ . This beta decay takes place via an allowed Gammow-Teller transition between the initial and final states.

- (a) What are the intrinsic spins and their relative alignment for the particles that are emitted from the nucleus in an allowed Gammow-Teller  $\beta^-$  decay?
- (b) Would you expect this beta decay to go directly from the ground state of the parent to the ground state of the daughter nucleus? Explain why or why not.
- (c) Suppose that some of the  $\beta^-$  decay goes to an excited state. What is the most likely decay mode of this state and how will the lifetime of this state compare to the  $\beta^-$  decay lifetime of the parent?
- (d) The beta decay of the daughter nucleus  $^{132}\text{Sb}$  has a significantly larger Q-value of 5508 keV even though it is “closer to stability.” This is an example of a general phenomena in the beta decay of nuclei with even mass numbers. Explain the basis for why the decay of this daughter has a larger Q-value than its parent decay.

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3. (10 points each) The A=132 mass chain accounts for 4.3% of the yield of fission fragments from the thermal-neutron fission of  $^{235}\text{U}$  and 4.95% from thermal-neutron fission of  $^{233}\text{U}$ .
- (a) (i) What is meant by the term “thermal neutron?” (ii) Give a detailed explanation of why these nuclei can undergo fission with a thermal neutron whereas the much more abundant uranium isotope,  $^{238}\text{U}$ , does not.
- (b) Use conservation of (1) momentum, (2) mass and (3) energy to make an estimate of the kinetic energy of an A=132 fission fragment from the fission of  $^{236}\text{U}$ . For this estimate you can ignore neutron emission, assume that the fissioning nucleus is at rest, and the energy released by the fission process is 200 MeV.